

TITLE OF THE INVENTION

TRACEABLE METHOD AND SYSTEM FOR ENCRYPTING AND/OR DECRYPTING
DATA, AND RECORDING MEDIA FOR IMPLEMENTING THE METHOD

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CROSS-REFERENCE TO RELATED APPLICATIONS.

STATEMENT REGARDING FEDERALLY SPONSORED RESEARCH OR
DEVELOPMENT.

10 _____ None.

THE NAMES OF THE PARTIES TO A JOINT RESEARCH AGREEMENT.

_____ None.

INCORPORATION-BY-REFERENCE OF MATERIAL SUBMITTED ON A COMPACT
DISC.

15 _____ None.

BACKGROUND OF THE INVENTION.

Field of the Invention.

20 The invention pertains to a traceable method and system for encrypting and/or
decrypting broadcast data, and to recording media for implementing the method.

More precisely, the invention concerns a traceable method in which:

- when encrypting broadcast data, the transmitter applies at least one first secret
cryptographic function, and

25 - when decrypting said broadcast data, all the decoders apply at least one same second
secret cryptographic function identical to said first function or its inverse, each decoder for
this purpose using a mathematical description of said second function recorded in a memory.

Traceable encrypting methods are methods in which a method for tracing traitors may
be implemented.

Description of Related Art

Traitor tracing methods are used to fight against the pirating of services which, on a broadcast channel, distribute encrypted multimedia contents such as video, television, images, music, texts, Web pages, electronic books, programmes etc. The purpose of traitor tracing methods is to prevent one or more lawful users of said services from re-distributing data deduced from the secret keys and decryption algorithms implanted in their decrypting equipment so as to enable unlawful users (pirates) to have in-clear access to said content. These methods guarantee that if such a fraud should occur, the identity of at least one of the lawful users at the source of the fraud may be reconstituted by the service operator distributing the content, or more generally by an authority, on the basis of data re-distributed to unlawful users. The lawful user at the source of the fraud is called a "traitor" in the remainder of the description.

The notion of tracing traitors was proposed for the first time by Benny Chor, Amos Fiat and Moni Naor in their 1994 article: "Tracing Traitors, Advances in Cryptology" – Crypto'94, Lecture Notes in Computer Science, vol. 839, Springer-Verlag, 1994, pp. 257-270. In this article, the first tracing techniques in a cryptographic system are put forward. The cryptographic systems in which a traitor tracing method may be implemented are called "traceable". Almost all these techniques are of combinatory nature. In other words, each lawful user of the cryptographic system is allotted a sub-set of keys of a set (generally a fairly large set) of basic keys. This sub-set of basic keys allotted to a user is unique for each user and forms the user's own personal key.

The data broadcast within this system comprises encrypted messages. Each encrypted message is formed of a content, encrypted by means of a content-encrypting key, and of headers each encrypted with a basic key. Each header contains a value representing part of the content-encrypting key.

When users receive one of these messages, they use their sub-set of basic keys to decrypt some values contained in the received headers. They then combine these decrypted values to reconstitute the content-encrypting key, and this reconstituted content-encrypting key is used to decrypt the content of the message.

If one of the lawful users of the system communicates his/her personal key to an unlawful user, then in this traceable cryptographic system it is possible to trace the identity of the traitor from the personal key used by the unlawful user.

However, traitor tracing methods of combinatory nature have the disadvantage of requiring the broadcasting of a considerable volume of headers. In particular, the number of headers to be broadcast is proportional to the logarithm of the number of lawful users of the system, and to other parameters such as the maximum size k of traitor coalitions against whom protection is sought. By coalition here is meant a group k of traitors who group together to combine their personal keys in an attempt to create a new personal key which can be used to decrypt the encrypted content, without examination of this new personal key disclosing the identity of one of the traitors.

The invention sets out to remedy this drawback by proposing a new traitor tracing method which does not require the broadcasting of a large number of headers.

BRIEF SUMMARY OF THE INVENTION.

The subject of the invention is therefore a traitor tracing method such as described above, characterized in that when implementing the second function, the mathematical description of this second function to which each decoder has recourse is different from one decoder to another or from one group of decoders to another, so that the mathematical description to which recourse is made exclusively identifies the particular decoder or group of decoders among all the decoders.

In the above method, it is possible to trace the traitor who communicated the mathematical description of his/her secret second function to an unlawful user, on the basis of analysis of the mathematical description of this second function used by the unlawful user to decrypt the transmitted data. Through the construction of each mathematical description in the system, said description represents the identity of the traitor. With the combinatory methods, on account of the fact that a personal set of keys is used in each decoder, the same content-encrypting key has to be transmitted several times encrypted in different forms. The headers placed at the start of the broadcast content are used for this purpose. Therefore the information contained in the headers is extremely redundant and each decoder only processes part of the received headers.

In the inventive method, on account of the fact that traitor identification is no longer based on the use of personal sets of keys but on use by the transmitter of different descriptions of one same cryptographic function, identical to the first cryptographic function, or its inverse, it is no longer necessary for at least part of the broadcast data to be redundant. Consequently the number of headers needed to broadcast an encrypted message using the

- functions g_1 are chosen so that each elementary function $G_{i,j}$ corresponds to an encryption block of a multivariate encryption algorithm;

- each function g_i is of the form $g_i(a) = a^{e_i}$, in which a is an element of an extension L' of degree n of a basic body L with q elements, and e_i is a predefined exponent;

- 5 - the exponent e_i is of the form $1 + q^{\theta_1} + \dots + q^{\theta_i} + \dots + q^{\theta_{d-1}}$, in which the exponents θ_i are predefined integers.

Another subject of the invention is a data recording medium, characterized in that it comprises instructions for executing a traceable method of the invention, when these instructions are performed by a decoder.

- 10 A further subject of the invention is a data recording medium, characterized in that it comprises instructions for executing a traceable method of the invention, when said instructions are performed by a transmitter.

- A further subject of the invention is a traceable encryption and/or decryption system for broadcast data capable of enabling the identification of a traitor, among different lawful
15 users, who has communicated secret data to a third non-authorized party enabling this third party to encrypt and/or decrypt broadcast data, this system comprising:

- a transmitter able to encrypt broadcast data, this transmitter being able to implement at least one first secret cryptographic function, and

- several decoders able to decrypt the broadcast data, all the decoders being capable of
20 implementing at least one same secret cryptographic function identical to said first function or its inverse, each decoder for this purpose being equipped with a memory in which a mathematical description of said second function is recorded;

- characterized in that the memory of each decoder contains a mathematical description of said second function different from the one recorded in the memory of the other decoders
25 or in the memory of the other groups of decoders, so that this mathematical description exclusively identifies the particular decoder or group of decoders among all the decoders.

- Finally, a further subject of the invention is a memory intended to be associated with a decoder of a traceable encryption and/or decryption system according to the invention, characterized in that it comprises a mathematical description equivalent to said second secret
30 function able to be used by the decoder, this mathematical description consisting of several elementary functions ($G_{i,j}$) each one equal to the composite of at least three functions as per one of the following equations:

By way of example, the transmitter 4 is a transmitter of paying television channels. This transmitter 4 comprises a module 10 for encrypting a content B_a and a module 12 for calculating a control word CW_a . Content B_a is here formed of a succession of data bits representing the television channels in clear, i.e. not encrypted.

5 Module 12 is able to execute a cryptographic function defined by a mathematical description F_K . This cryptographic function is intended to directly process a header EB_a coded over n characters to convert it into a control word CW_a also coded over n characters, n being a strictly positive integer greater than 100 for example. Here, by way of example, each character is either a "0" or a "1".

10 For this purpose, the transmitter 4 is associated with a memory 14 in which the mathematical description F_K of the cryptographic function is recorded. A mathematical description is a set of data determining the exact sequence of mathematical operations to be conducted in order to calculate, for every input value, the corresponding output value of this function, without any value other than the input value of the function having to be provided
15 to the programme to conduct the calculations. This description F_K is recorded in the memory 14 in a format which can be directly used by the transmitter so that module 12 is able, on the basis of this description, to perform its cryptographic function. Here, for example the description F_K is a sequence of instructions forming a computer programme. However, in the remainder of this description, the mathematical descriptions of the functions will be solely
20 shown in the forms of mathematical relations expressed using conventional symbols. The computer programme or programmes corresponding to the mathematical relations described below are easy to write.

The description F_K will be described in more detail with respect to figure 2.

25 Module 10 is able to execute an encryption function E parametered by the control word CW_a constructed by module 12 in order to encrypt content B_a and to output a corresponding encrypted content CB_a . The encryption function E here is a conventional invertible encryption function. It is for example an AES encryption function (Advanced Encryption Standard) or the encryption algorithm known under the name "one time pad".

30 For each content B_a encrypted by module 10 using the control word CW_a , the transmitter 4 is able to broadcast a data pair towards all the decoders in the system. This data pair is formed by the header EB_a and the encrypted content CB_a .

To decrypt the data transmitted or broadcast by the transmitter 4 through the network 6, the decoder 8 comprises a calculation module 20 to calculate the control word CW_a and a decryption module 22 to decrypt the encrypted content CB_a .

Module 20 is able to execute a cryptographic function. This function is defined by a mathematical description F_{Kj} different from description F_K . More precisely, this description F_{Kj} is different from all the descriptions F_{Kj} used in the other decoders of the system 2. However, even though the mathematical description F_{Kj} is different from description F_K , the function it defines is the same. Consequently, the conversion of the header EB_a by module 20 makes it possible to obtain the control word CW_a , i.e. the same as the one which would have been obtained using module 12. Under these conditions, the description F_{Kj} is said to be equivalent to description F_K .

Similarly to transmitter 4, the decoder 8 is associated with a memory 21 in which the mathematical description F_{Kj} is recorded.

The description F_{Kj} will be described in more detail with respect to figure 2.

Module 22 is able to execute a decryption function D. This function D is the inverse of function E making it possible to decrypt content CB_a using the control word CW_a constructed by module 20 on the basis of the received header EB_a .

The decoder 8 is also able to transmit the content B_a decrypted by module 22 to a television set 26 on which it is displayed in clear.

The transmitter 4 and each of the decoders are based on conventional programmable calculators able to execute instructions recorded on a data recording medium. For this purpose, the memories 14 and 21, in addition to the secret parameters for encrypting and decrypting transmitted data, contain instructions for execution of the method in figure 2.

The functioning of the system 2 will now be described with reference to the method of figure 2.

The method in figure 2 is divided into three main phases. A set-up phase 50 of system 2, a use phase 52 of system 2 and finally a search phase 54 to search a traitor among the different lawful users of the system 2.

Phase 50 starts with a construction step 60 to construct the mathematical description F_K . For this purpose, r non-linear functions g_i are constructed during an operation 62, r being

a strictly positive integer. The number r of functions g_i is chosen so as to verify the following relationship:

$$(1) \quad N < r !$$

in which N is the number of decoders in system 2.

- 5 These functions g_i are constructed so as to be commutative between each other, through the composition operation, so that the following relationship is verified:

$$(2) \quad \forall i, 1 \in \{1, \dots, r\}, i \neq 1 \quad g_i \circ g_1 = g_1 \circ g_i$$

in which the symbol \circ represents the composition operation of two mathematical functions.

- 10 Here, each of these functions is a non-linear function converting a tuple into another tuple. By tuple is meant here a set of n elements. For example the set of n coefficients of a polynomial of degree $(n-1)$ may be considered a tuple.

- Therefore, each function g_1 takes n input variables and outputs n calculated variables. Here they each correspond to a system of n non-linear equations with n variables, n is a strictly positive integer which here corresponds to the number of characters of the header EB_a .

- Here, each function g_1 is chosen to form an encryption block G_1 of a multivariate encryption algorithm, when it is composed on the right and left with linear functions. An example of multivariate encryption algorithm is for example the C^* algorithm proposed by
- 20 Matsumoto and Imai in Tsutomu Matsumoto and Hideki Imai, "Public Quadratic Polynomial-tuples for Efficient Signature Verification and Message Encryption, Advances in Cryptology" – EUROCRYPT '88 (Cristoph G. Günther, ed), Lecture Notes in Computer Science, vol. 330, Springer, 1988, pp. 419-453). Other examples of multivariate encryption algorithms are the algorithms known under the names SFLASH v2 (NESSIE project, New
- 25 European Schemes for Signatures, Integrity and Encryption) and HFE (PATARIN Jacques Hidden Fields Equations (HFE) and Isomorphisms of Polynomials (IP): two new families of Asymmetric Algorithms (Eurocrypt 96, Springer Verlag, pp. 33-48).

- So as to obtain from elements g_i a description that is both simple and compact of the resulting encryption blocks G_i , the g_i functions are chosen as being monomial functions,
- 30 called monomes.

As an example, here each of the functions g_i operates on the elements an extension L' of degree n of a base body L with q elements. For example here $q = 2$ and $L = \{0, 1\}$.

Extension L' is shown as the set of polynomials of form:

$$\sum_{i=0}^{n-1} a_i X^i$$

in which:

- the coefficients are elements of the body L
- 5 - the index i is an integer, and
- X is a variable.

Extension L' is provided with the addition of polynomials and with multiplication modulo an irreducible polynomial of degree n defined by the following equation:

$$P(X) = \sum_{i=0}^{n-1} p_i X^i$$

10 in which:

- the coefficients p_i are predefined elements of body L , and
- X is a variable,

As an example, the g_i functions are functions of extension L' in extension L' of the form: $g_i(a) = a^{e_i}$

15 in which:

- a is an element of extension L' , and
- the exponent e_i is a predefined integer of the form $1 + q^{\theta_1} + \dots + q^{\theta_i} + \dots + q^{\theta_{i-1}}$, in

which q is the number of elements of body L and the exponents θ_i are predefined integers.

Here d is chosen to be equal to 2 so that the exponent e_i of each of the functions g_i has
20 the form $1 + q^{\theta_1}$.

The advantage of an exponent e_i in this form is that if each element a of extension L' is identified with tuples $(a_0, a_1, \dots, a_{n-1})$ of coefficients, each of coefficients b_0, b_1, \dots, b_{n-1} of element b of extension L' defined by the equation $b = g_i(a)$ is written as a function of degree d only of coefficients a_0, a_1, \dots, a_{n-1} of a . That is to say, here, as a quadratic function in the particular case when d equals 2. In this particular case, each coefficient b_i may be written in the form of the following quadratic function:

$$b_i = (c_{0,0} a_0 + \dots + c_{n-1,0} a_{n-1}) + (c_{0,1} a_0 a_1 + \dots + c_{0,n-1} a_0 a_{n-1}) + (c_{1,2} a_1 a_2 + \dots + c_{1,n-1} a_1 a_{n-1}) + \dots + c_{n-2,n-1} a_{n-2} a_{n-1}$$

in which the n coefficients c_n and the $n(n-1)/2$ coefficients $c_{u,v}$ are constants belonging
30 to the body L .

$G_{r,j} = T \circ g_{\sigma_j(r)} \circ f_{r-1,j}$
 in which:

- $f_{i,j}^{-1}$ is the inverse of bijection $f_{i,j}$, and
- $g_{\sigma_j(t)}$ is function g_i whose index i is equal to the permute of index t by permutation

5 σ_j of user j , t belonging to the set $\{1, 2, \dots, r\}$.

The property of function g_i according to which each coefficient b_i of element b of extension L' defined by the equation $b = g_i(a)$ may be written as a polynomial of degree d only, is conserved when function g_i is composed on the right and left by bijections or linear functions. Therefore, the components of element y of L^n defined by the equation $y = G_{i,j}(x)$ may be described by a polynomial of degree d only of the components x_i of element x of L^n . For example when d equals 2, the component y_i is defined using the following mathematical description:

$$y_i = (c'_{i,0} x_0 + \dots + c'_{i,n-1} x_{n-1}) + (c'_{i,0,1} x_0 x_1 + \dots + c'_{i,0,n-1} x_0 x_{n-1}) + (c'_{i,1,2} x_1 x_2 + \dots + c'_{i,1,n-1} x_1 x_{n-1}) + \dots + c'_{i,n-2,n-1} x_{n-2} x_{n-1}$$

15 in which the n coefficients $c'_{i,u}$ and the $n(n-1)/2$ coefficients $c'_{i,u,v}$ are constants belonging to body L .

Therefore by means of the choice of exponent e_i in the form $1 + q^{e_i}$, the mathematical description of each elementary function $G_{i,j}$ is simple and compact and hence takes up little memory space. In particular, in the embodiment described here, the mathematical description of each elementary function $G_{i,j}$ is a system of n non-linear equations with n variables.

The description F_{Kj} is formed by these r elementary functions $G_{i,j}$. By processing the input message with the equation (5): $F_{Kj} = G_{r,j} \circ G_{r-1,j} \circ \dots \circ G_{2,j} \circ G_{1,j}$, exactly the same output message is obtained as the one which would have been obtained using description F_K . The equivalence of the mathematical descriptions F_{Kj} and F_K is easy to verify by replacing, in the preceding equation, each elementary function $G_{i,j}$ by its definition given by equation (4). By so doing in the previous equation, we obtain:

$$F_{Kj} = T \circ g_{\sigma_j(r)} \circ g_{\sigma_j(r-1)} \circ \dots \circ g_{\sigma_j(2)} \circ g_{\sigma_j(1)} \circ S$$

Since all the g_i functions are commutative between each other, it is therefore shown that description F_{Kj} is equivalent to description F_K .

It is therefore understood that the function of the bijections $f_{i,j}$ is to make the elementary functions $G_{i,j}$ non-commutative between each other. In this case, to obtain an equivalent description to description F_K , the elementary functions $G_{i,j}$ can only be composed with one another in the increasing order of their index i as in equation (5).

- 5 In addition, the sturdiness of the system against any attempted cryptanalysis, in the particular embodiment described herein, is based on the difficulty of the isomorphisms of polynomials, also known as the IP problem. With knowledge of the $G_{i,j}$ functions, it is mathematically very difficult, even with knowledge of all the functions g_1 to g_n , to identify the values $\sigma_j(i)$ since unknown functions are used in each elementary function $G_{i,j}$ for their camouflaging by composing on the right and left. Here, these unknown functions are 10 functions S and T which are kept secret and the bijections $f_{i,j}$. Whereupon it is not possible for an unlawful user possessing a set of valid elementary functions $G_{i,j}$ to construct a new set of elementary functions $G'_{i,j}$ in which the order relationship defined by σ_j between the g_i functions is not maintained. In other words, since the unlawful user is incapable of finding 15 functions S , T and $f_{i,j}$ from the elementary functions $G_{i,j}$ said user must be content with modifying the mathematical description of each elementary function $G_{i,j}$ without being able however to modify the order in which these elementary functions must be combined. Therefore since the order in which the elementary functions $G'_{i,j}$ are combined is not modified, the order in which the functions g_i are combined is not modified either. The 20 advantage of this property will become apparent on reading the remainder of the description.

Once the elementary functions $G_{i,j}$ have been constructed for each user j of system 2, they are distributed and recorded, during step 80, in the memory 21 of each decoder 8 in the form of a computer programme for example.

- Also, during this step 80 the information necessary for executing traitor search phase 25 54 is recorded in memory 14 for example. In particular, all the functions used to construct each elementary function $G_{i,j}$ are recorded in this memory 14 and each of the permutations σ_j used. The relationship between each permutation σ_j and the decoder for which it has been used is recorded. Similarly a relationship enabling identification of a user from the identity of the decoder is recorded in this memory 14.

Once functions G_{ij} have been recorded in the memory of each decoder 8, the use phase 52 of system 2 can be initiated.

During this phase 52, the transmitter 4 randomly draws a new header EB_a during step 84 at regular intervals, for example every second.

5 This header EB_a is converted during step 86 by module 12 using description F_K in order to obtain the control word CW_a .

Content B_a is then encrypted by module 10 during a step 88 using function E and the control word CW_a . The encrypted content CB_a and the header EB_a used for this purpose are then broadcast conjointly, during step 90, by transmitter 4 through the network 6 towards all the decoders within system 2.

10 On receipt of the encrypted data, each decoder firstly proceeds during step 92 with calculating the control word CW_a from the received header EB_a . During this step, the module 20 successively uses, and in order, each of the elementary functions G_{ij} recorded in its memory 21, so as to perform the calculation corresponding to the composite of the elementary functions G_{ij} in accordance with equation (5).

After this step 92, the module 20 outputs the same control word CW_a as the one constructed by module 12 of transmitter 4.

Using this control word CW_a and function D , the module 22 during step 94 decrypts the received encrypted content CB_a . The decrypted content B_a delivered by module 22 is then transmitted for in-clear display to a television set 26 for example.

Steps 84 to 94 are repeated throughout the entire use phase of system 2 for each data item or data frame broadcast by transmitter 4.

For the remainder of the description, it is assumed that the user of decoder j has transmitted to an unlawful user his set of elementary functions G_{ij} so that this unlawful user is able to use a pirate decoder to decrypt the data broadcast by the transmitter 4 without having to pay a subscription for example. The user of decoder j is therefore the traitor since he has illegally and unlawfully transmitted secret data allowing decryption of data broadcast by transmitter 4.

30 Traitor search phase 54 starts by capturing and analysing, during step 100, a pirate decoder of the unlawful user. During this step 100, analysis of the decoder is made so as to

detect therein the elementary functions $G_{i,j}$ unlawfully communicated to it by the traitor, and the order in which these functions $G_{i,j}$ are combined to convert the received header EB_a into a control word CW_a .

5 The elementary functions found in the pirate decoder are here noted $G_{i,p}$ in which the index i indicates the order in which these elementary functions are used to convert the control word EB_a .

Subsequently each function $G_{i,p}$ is analyzed during step 102 to find the function g_i on the basis of which it was constructed. Said analysis is possible for example for the operator of system 2 since the operator knows the functions S , T , $f_{i,j}$ and g_i used to construct the elementary functions $G_{i,j}$ of each user of the system.

10 Therefore after step 102, the operator of the system 2 is capable of saying that the elementary function $G_{1,p}$ was constructed from function g_m , that the elementary function $G_{2,p}$ was constructed from function g_n and so on for each of the functions $G_{i,p}$ in which the indices m and n of functions g_m and g_n represent the index of the function g_1 used to construct $G_{1,p}$ and $G_{2,p}$ respectively.

On the basis of this information, the operator is therefore able, during step 104, to reconstruct the permutation σ_j used during the construction of the elementary functions $G_{1,p}$ used in the pirate decoder. Once this permutation σ_j is reconstructed, it is compared during step 106 with different permutations recorded in memory 14 during step 80.

20 By means of the above the traitor, i.e. the user of decoder j , is identified since in system 2 each permutation σ_j corresponds to a single decoder itself associated with a single user.

This system and this method therefore prove to be particularly dissuasive to prevent lawful users from communicating the necessary data for decrypting encrypted contents CB_a .

25 Studies of the sturdiness of the method in figure 2 against attempted cryptanalysis have been conducted. These studies have shown in particular that the system and the method of figure 2 resist against attacks led by a coalition of k traitors, k being a positive integer greater than two. By coalition of k traitors is meant here a group of k lawful users who attempt, by pooling their respective sets of elementary functions $G_{i,j}$, to construct a new equivalent description of function F_k . It was shown that these unlawful users are able at the

most to construct a function using one or more new sets of elementary functions $G_{i,p}$ from these k sets of elementary functions $G_{i,j}$. However any new set of elementary functions $G_{i,p}$ results from the combination of successive sequences of elementary functions $G_{i,j}$ extracted from each of the sets of elementary functions at its disposal. For example for a coalition of

5 two traitors, the new set of elementary functions $G_{i,p}$ which an unlawful user could construct would be composed of the p first elementary functions $\{G_{1,1}, G_{2,1}, \dots, G_{p,1}\}$ of the first traitor and of the $r-p$ last elementary functions $\{G_{p+1,2}, \dots, G_{r,2}\}$ of the second traitor. To combat said attempted camouflaging of the traitor's identity, the number r of functions g_i is chosen to be sufficiently high so that at least one traitor can be identified solely on the basis

10 of the identification during phase 54 of only part of the permutation σ_j used to construct his set of elementary functions $G_{i,j}$. For example, for a coalition of two traitors, r is chosen to be sufficiently high so that at least one of the traitors can be identified either on the basis of the p first elementary functions $G_{i,1}$ or on the basis of the $r-p$ last elementary functions $G_{i,2}$.

It will be noted in the above method that the same secret data, i.e. the cryptographic

15 functions associated with descriptions F_K, F_{Kj} are used to encrypt and decrypt so that the described encryption method has the same characteristics as an algorithm of symmetric encryption. In particular, by means of this property, the method described here is quicker than an algorithm of asymmetric encryption.

Here the functions $S, T, f_{i,j}$ must be kept secret, whilst the functions g_i are optionally

20 published.

In system 2, only one same function for calculating the control word CW_a is used both in the transmitter 4 and in the decoders. Therefore this cryptographic function does not need to be invertible which facilitates the choice and construction of functions g_i . However, as a variant, the description F_K corresponds to an encryption function and descriptions F_{Kj}

25 correspond to the inverse of this encryption function. In this variant, the different descriptions F_{Kj} implanted in the different decoders of the system are equivalent to one another and are descriptions equivalent to the inverse of the function defined by description F_K . The previously described construction of descriptions F_{Kj} applies, the only difference being that functions g_i must be invertible in this variant. In this case the description F_K is for example

used to encrypt content B_a directly, whilst the equivalent descriptions F_{kj} are used to decrypt encrypted contents CB_a directly.

Here the cryptographic function corresponding to descriptions F_k and F_{kj} converts an initial message coded over n characters into a converted message also coded over the same number of characters. This cryptographic functions does not increase the size of the converted message with respect to the size of the initial message, contrary to the finding with asymmetric algorithms for example. As a variant, the cryptographic function increases the size of the converted message with respect to the size of the initial message. It will be noted however that in this variant this increase in size remains independent from the number of
10 traitors.

System 2 has been described in the particular case in which a description F_{kj} is associated with a single decoder. As a variant, one same description F_{kj} is associated with a group of decoders. In this variant, all the decoders of system 2 are grouped together in several groups so that the description F_{kj} identifies not a particular decoder but the group to which
15 this particular decoder belongs.

20